

King Abdulla II School for Information Technology  
Department of Computer Science  
Numerical Analysis - MidTerm - Spring 2013

Student Name:

Student ID:

Section:

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**Q1 (2 Points)** let  $a = 0.471 * 10^{-2}$  and  $b = 0.869 * 10^4$ . Use 3 digits arithmetic to show that the computed value  $a + b$  is equal to  $b$ .

**Q2 (4 Points)** Consider the linear system

$$AX = \begin{bmatrix} 4 & -1 & 2 \\ 0 & 3 & 1 \\ 0 & 0 & 2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 7 \\ 5 \\ 4 \end{bmatrix} = B$$

(a) Use back substitution to solve the system

(b) Compute  $\det(A)$

**Q3 (2 Points)** Let

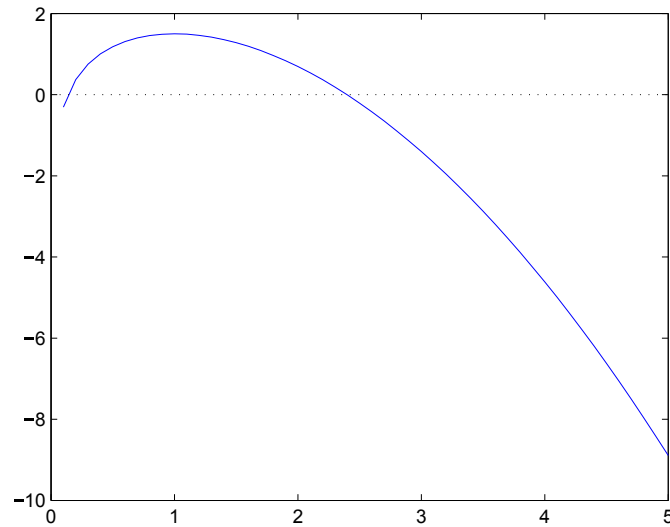
$$X = \begin{bmatrix} 3 \\ -5 \\ 0 \end{bmatrix}, \text{ and } Y = \begin{bmatrix} 2 \\ 1 \\ -3 \end{bmatrix}$$

Compute

(a)  $\|X\| =$

(b)  $XY =$

**Q4 (4 Points)** Consider the function  $f(x) = \ln x + 2 - \frac{x^2}{2}$  whose graph is given below.



- (a) On the graph, illustrate how Newton-Raphson method locates  $p_1$  starting with  $p_0 = 4$ .
- (b) With  $p_0 = 1$ , will Newton-Raphson method converge to a root?

**Q5 (4 Points)** Consider the fixed point iteration

$$p_{k+1} = 2p_k - \alpha p_k^2, \quad \text{for } k = 0, 2, \dots$$

where  $\alpha > 0$  is given. Show that the iteration converges for any initial guess  $p_0$  satisfying  $0 < p_0 < \frac{2}{\alpha}$

**Q6 (6 Points)** Consider approximating the positive root of  $x^2 - 3 = 0$ .

(a) Using the bisection method and starting with the interval  $[1.5, 2.5]$ , how many iterations would be necessary to ensure the root is bracketed in an interval of length less than  $10^{-3}$ ?

(b) Using the method of fixed point iterations,  $p_n = g(p_{n-1})$  with  $g(x) = \frac{3}{x}$ , will convergence occur starting with the initial guess  $p_0 = 2$ ?

(c) Starting with  $p_0 = 2.0$ . Use Newton-Raphson method to compute  $p_1$  and  $p_2$ .